

College Algebra
Formula Sheet for Test 5

Binomial Theorem

$$\begin{aligned} [(1^{\text{st}} \text{ term}) + (2^{\text{nd}} \text{ term})]^n &= (1^{\text{st}})^n + {}_n C_1 (1^{\text{st}})^{n-1} (2^{\text{nd}})^1 + {}_n C_2 (1^{\text{st}})^{n-2} (2^{\text{nd}})^2 + \dots \\ &+ {}_n C_{n-1} (1^{\text{st}})^1 (2^{\text{nd}})^{n-1} + (2^{\text{nd}})^n \\ \text{rth term} &: {}_n C_{r-1} (1^{\text{st}})^{n-(r-1)} (2^{\text{nd}})^{r-1} \end{aligned}$$

Sequences

Arithmetic: Explicit $\rightarrow a_n = a_1 + (n-1)d$

Recursion $\rightarrow a_n = a_{n-1} + d$

Geometric: Explicit $\rightarrow a_n = a_1(r^{n-1})$

Recursion $\rightarrow a_n = (a_{n-1})r$

Series

Recursion $\rightarrow S_n = S_{n-1} + a_n$

Arithmetic: Explicit $\rightarrow S_n = \left(\frac{n}{2}\right)(a_1 + a_n)$

$$S_n = \left(\frac{n}{2}\right)[2a_1 + (n-1)d]$$

Geometric: Explicit $\rightarrow S_n = \frac{a_1(1-r^n)}{1-r}, \quad 1 \neq r$

$$S_n = \frac{a_1 - (a_n)r}{1-r}, \quad 1 \neq r$$

Infinite Geometric : $S_\infty = \frac{a_1}{1-r}, \quad |r| < 1$